## Mathematics for Systems Biology and Bioinformatics Lecture Prof. Dr. Thomas Filk Tutorials Dr. Tim Maiwald, Christian Tönsing

Exercise sheet no. 5 Submission until 28. Nov 2012 10:00 am in the tutorials

## Exercise 7: Adjacency Matrix I

Consider a graph of a system

$$a \to b \to c$$

with its adjacency matrix

$$A = \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 0 \end{pmatrix}$$

where entries  $a_{ij}$  represent a directed link from *i* to *j*.

a) Given vector  $v_0 = (10, 2, 0)$  as a starting value for the species a, b and c, calculate  $v_1 = v_0 \cdot A$  and  $v_2 = v_1 \cdot A$ . Discuss the result.

b)  $A^k = \underbrace{A \cdot A \cdot \ldots \cdot A}_{k \text{ times}}$  presents every link in the graph over k edges. Calculate  $A^2$ .

## Homework 7: Adjacency Matrix II (4 Points)

a) Calculate the above exercises and draw the according graph of the system of the adjacency matrix

$$B = \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{pmatrix}$$

b) For the system

$$\begin{array}{c} a \rightarrow b \\ a \rightarrow c \rightarrow d \rightarrow b \end{array}$$

find the adjacency Matrix C and prove that the graph contains no path over more than 3 edges. c) For the system

$$\begin{aligned} a \to b \to b \\ a \to c \to d \to b \end{aligned}$$

find the adjacency Matrix C. Consider starting values  $v_0 = (7, 0, 0, 0)$  and calculate  $v_3$ . Find a simple way to modify the system such that  $v_3 = (0, 7, 0, 0)$ , using the same starting values  $v_0$ . *Hint:* You may exchange '1' in the adjacency matrix by any suitable number.

## Homework 8: Analysis of Stability (6 Points)

Given r and l constant parameters over time, starting value  $x_0, r, l \in \mathbb{R}^{\neq 0}$ 

a) Calculate the fix points and find a generally accepted solution for any  $x_n$ .

$$x_{n+1} = r \, x_n$$

b) Calculate the fix points. Discuss cases  $x_{n+1} > x_n$  and  $x_{n+1} < x_n$  and set in biological perspective.

$$x_{n+1} = r x_n - l$$

c) Calculate the fix points. *Hint:* The solution includes a special case.

$$x_{n+1} = r x_n - l \sin(n)$$

d) Find fix points. How could you change the equation by adding one term to create a fix point for r = l?

$$x_{n+1} = r x_n \sin(n) - l x_n \sin(n)$$